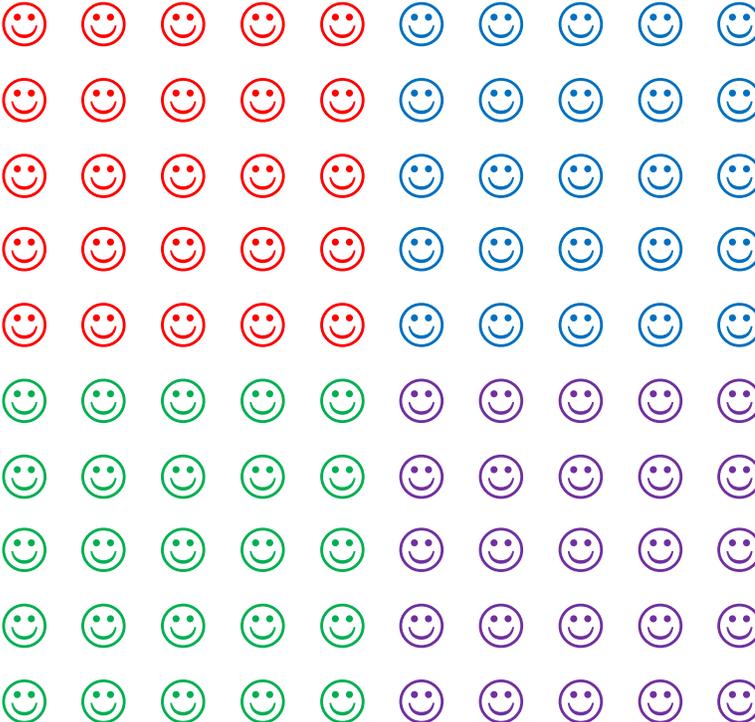
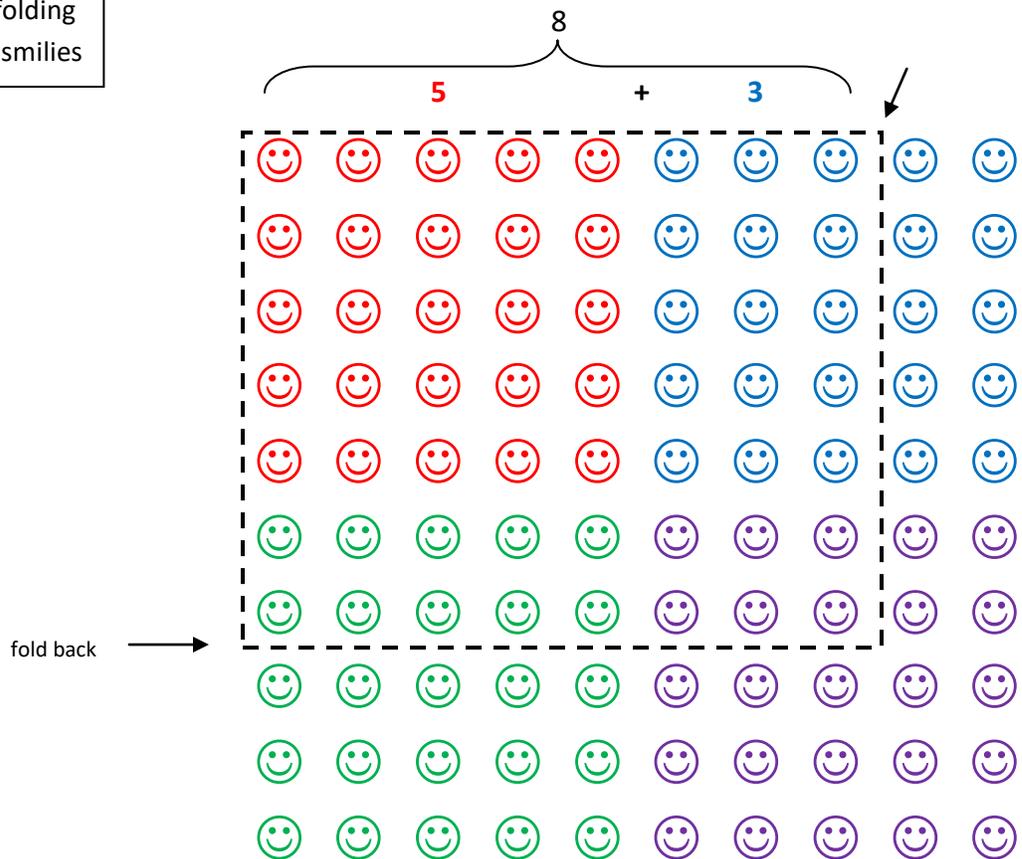


# Happy Hundred and Tweaky Twelve foldable multiplication template



Example: find  $7 \times 8$  by folding an array of 7 rows of 8 smilies



- Goals:**
- connect multiplication to the five times table,
  - learn to decompose factors for multiplication,
  - become familiar with counting different groups: groups of 5, later groups of 10
  - understand the box method of multiplication to use it with extended notation,
  - show the relationship with multiplication of mixed numbers and polynomials (FOIL) in algebra.

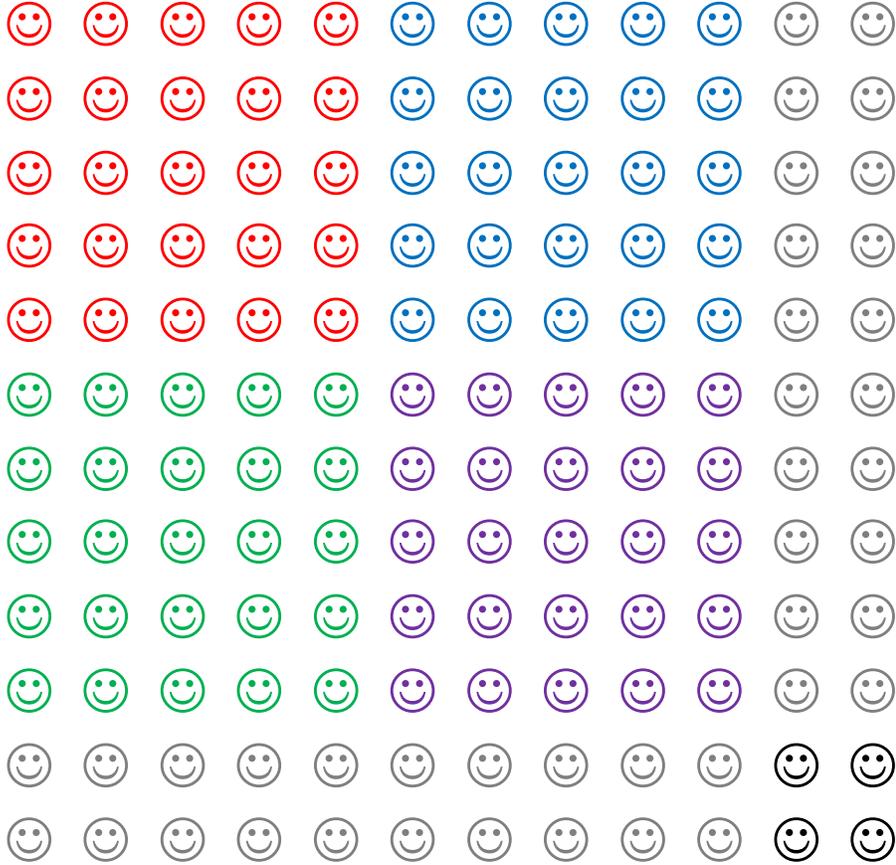
**How to multiply with the Happy Hundred and Tweaky Twelve** Basically we use the easy five times table to do other multiplications. Example: what is  $7 \times 8$  or 7 rows of 8, see the dotted rectangle above. Student folds back on the dotted lines, so you see the  $7 \times 8$  array. Ask: "How many groups of five do you see? Remember: the fives can be horizontal and vertical." Shapes that show 5 such as the yellow 5-rods (Cuisenaires) help count groups of 5. Fill up the whole array with rods and ones, a rods track shows total.

You see **5 red vertical columns of five**, **3 blue vertical columns of five**, and **2 green horizontal groups of five**, so  $5 + 3 + 2 = 10$  groups of 5 = 50. There are  **$2 \times 3 = 6$  purple smilies**. Total =  $50 + 6 = 56$ , so  $7 \times 8 = 56$ .

**Decompose factors:** decompose 7 into  $5 + 2$ , draw a box around the colors, do  $5 \times 8 = 40$  first and then  $2 \times 8 = 16$ . Ask: "what is 5 eights + 2 eights together?" Yes, that's 7 eights, or  $40 + 16 = 56$ , so  $7 \times 8 = 56$ .

**Hands-on multiplication of mixed numbers and polynomials** Come back to this familiar model to teach multiplication of mixed numbers and polynomials: decompose mixed number in whole number + fraction, model one whole with a square that covers 25 smilies and  $\frac{1}{5}$  that covers 5 smilies, write the factors on the outside. After student has worked with the hands-on model, use the box method for more combinations. FOIL: Model  $X^2$  with a square that covers 25 smilies and model  $X$  with a rectangle that covers 5 smilies, write factors on the outside and introduce different color algebra tiles for positive and negative, such as blue/green for pos. vs. red for neg. After hands-on, use the box method for FOIL.

## Tweaky Twelve multiplication



Find groups of ten, groups of five, and ones

Multiply ..... rows of ..... smileys each:

there are ..... groups of 10 = ..... ones

..... groups of 5 = ..... ones

and ..... ones

total: .....