

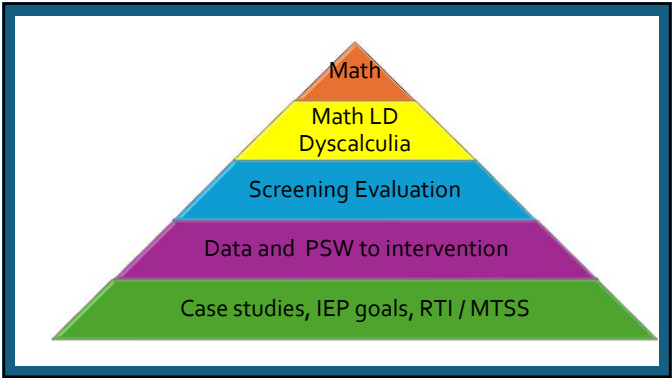
FROM IDENTIFICATION TO
INTERVENTION:
SUPPORTING STUDENTS WITH A
MATH LD OR DYSCALCULIA

REGION 2 CORPUS CHRISTI 6/3/2026

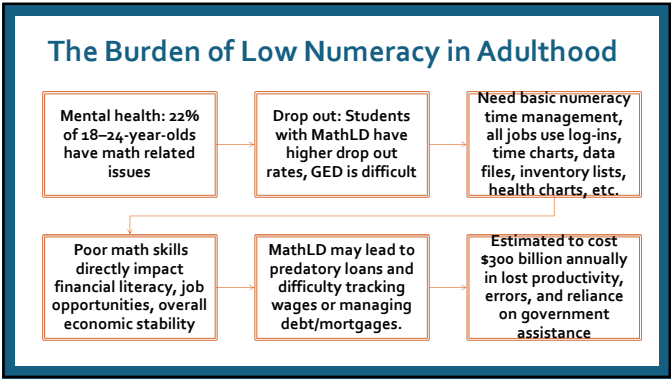


Dr. Anneke M. Schreuder
drschreuder@dyscalculiaservices.com
DyscalculiaTutorTraining.org

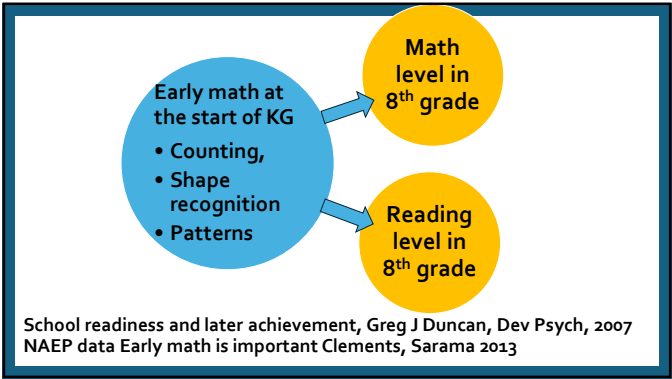
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3



4

Processing issues

Attention issues

Anxiety

Low numeracy

Teaching issues

Visual Spatial issues

Memory issues

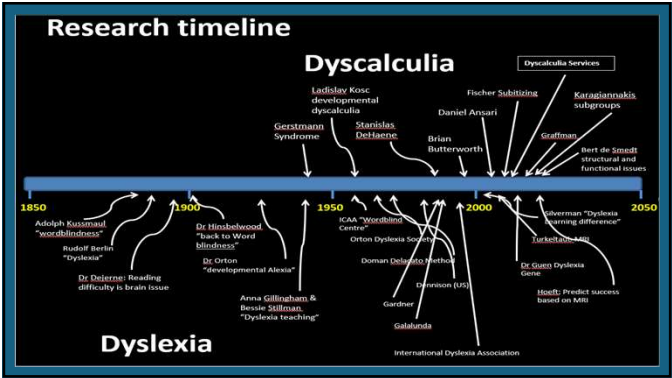
Language issues

Dyscalculia

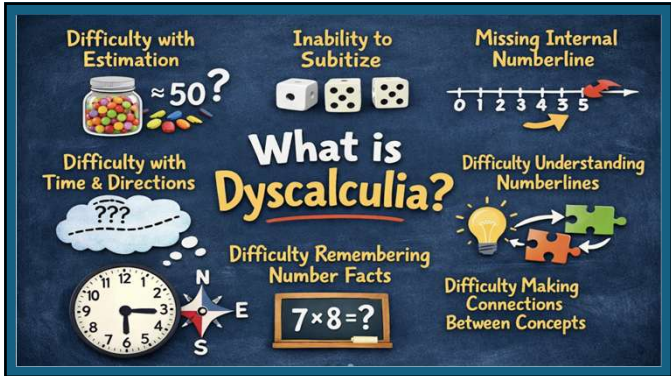
What could cause math problems?



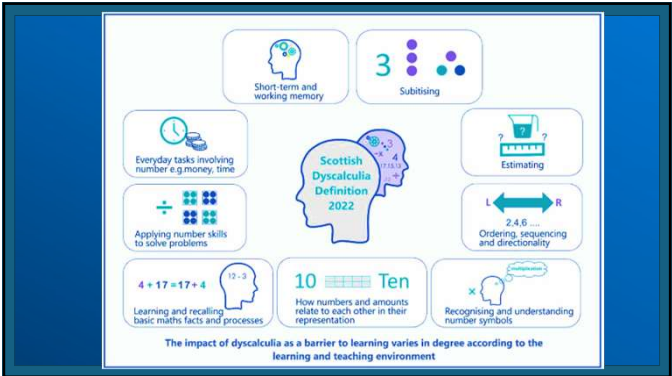
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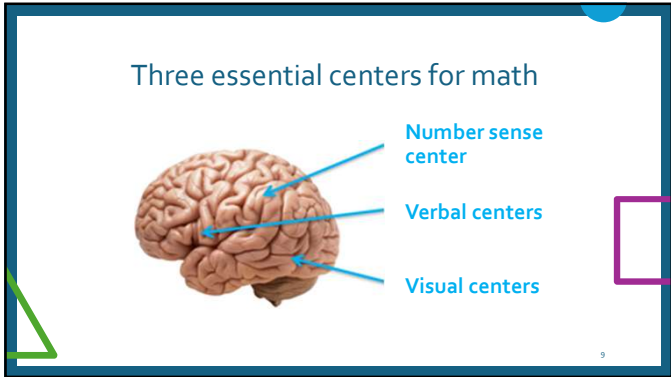
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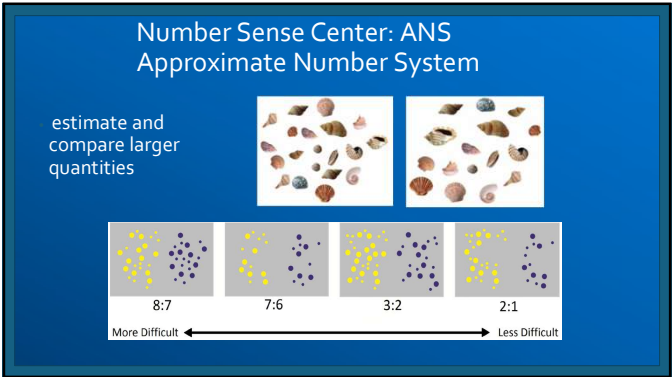
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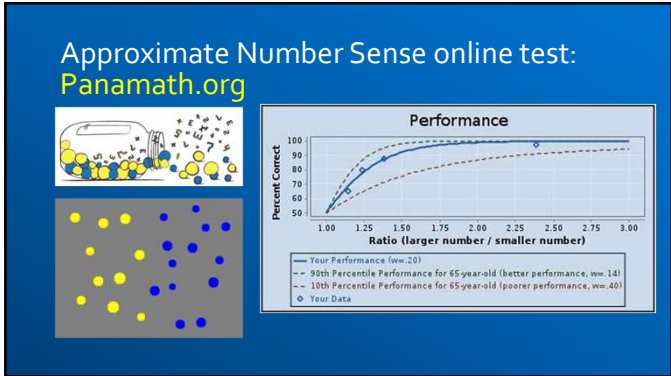
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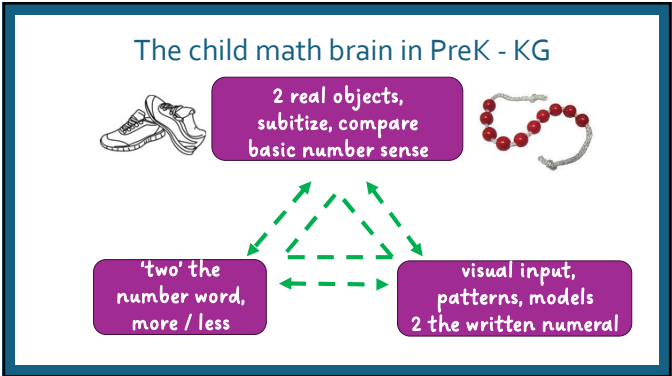
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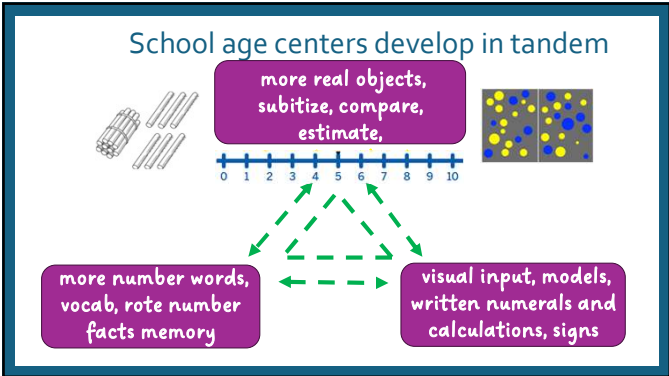
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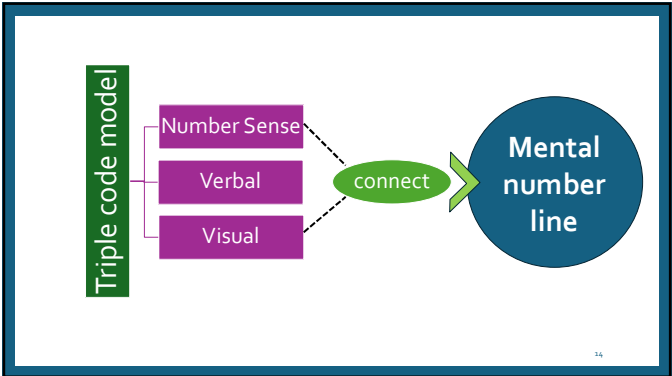
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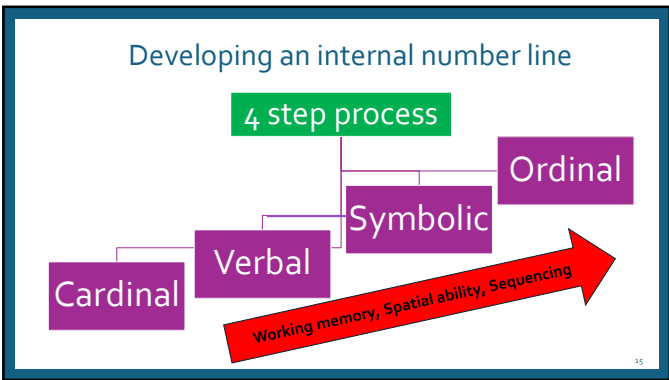
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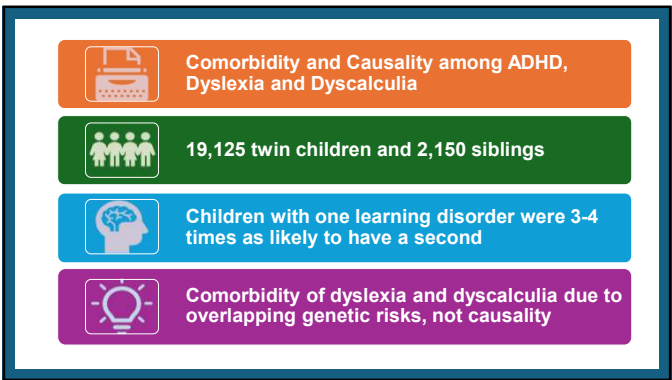
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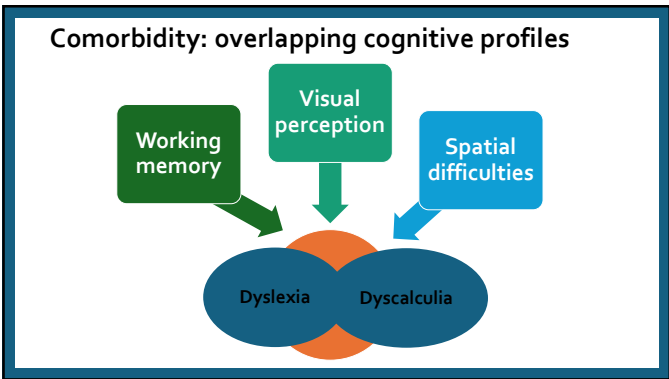
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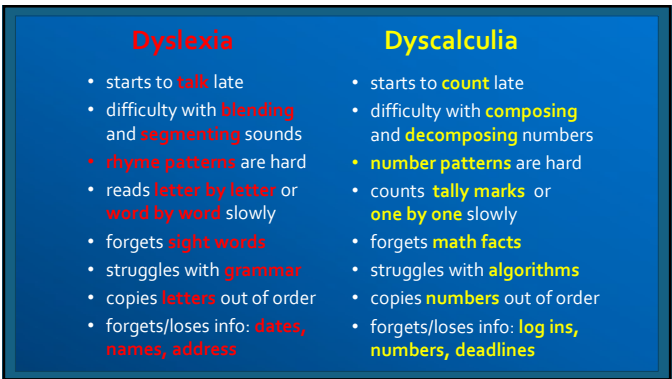
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Language

- Phoneme:** individual sounds
- Phonemic awareness:** awareness of sounds within words
- Phonological awareness:** knowledge and sensitivity to phonological structure of words (rhyme, syllable count, first, middle, and ending sound)
- Phonics letter-sound association:** teaching reading and spelling using sound-symbol connection

Math

- Unit of counting:** dots, beads, etc.
- Part-Whole awareness:** smaller numbers exist within a number
- Number Sense:** knowledge and sensitivity of the structure of numbers, more/less, part-whole, grouping, place value
- Written numeral - number word - quantity association:** teaching connection of real quantities with number words and numerals

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Language

- Decoding** sound out a word using letter-sound connection, digraphs, syllables structures
- Sight words** like in the Dolch list, some need to be memorized, some can be derived
- Spelling** as encoding
- Sentence writing** verbal content to convey meaning
- Comprehension** from learning to read to reading to learn and make sense of a text

assessment

Math

- Decoding** numerals using the triple code and place value groups as 'syllables'
- Math facts** can be memorized, many can be derived using the number structure
- Writing a quantity** as encoding
- Calculations** number sentences to convey quantitative meaning
- Problem Solving:** apply number knowledge and structure to make sense of a word question

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Math LD and dyscalculia diagnosis gap

The Language Barrier ELL

Math struggles can be misinterpreted as language hurdles.

Misattributing Struggles

- Seemingly inattentive mistakes mask misunderstanding
- It is 'just developmental'
- Not trying hard enough, etc.

Diagnostic Overshadowing

- Through comorbidity of dyscalculia, other LDs or ADHD
- Schools can only address one LD at a time

Referral and Identification Delay

- 1st or 2nd grade is deemed 'too early' to assess / diagnose
- Need to fail twice first

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Possible causes of math anxiety

Difficult timed tests and pop quizzes

Being called upon to answer a problem

Working under time pressure

Start new concept before the previous is understood

Tests that cover multiple topics, benchmarks

No visual cues or modeling

Not understand notes and need to do HW.

Abstract, no concrete or representation

Only one algorithm accepted

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Student stress respond behaviors

Fight	Flight	Freeze	Fawn
Aggression Arguing Threats Yelling Cursing Refuse to sit at desk Provoke adults	Walk out of class Ignore teacher Skip classes Getting kicked out on purpose Headphones Cellphone surfing	Blankly staring Dissociating Shrug Head on desk Not answering Appear forgetful absent minded Avoiding tasks	Perfectionism Overpreparing Befriending bullies Submit to pressure Lack boundaries People pleasing

Building a Trauma Restorative School, Brummer, 2011

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mAMAS Math Anxiety Score, age 8-13, 9 questions
Emma Carey et al, Frontiers of Psychology 2017, vol. 8

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Early screening in KG – 1st grade

- ❖ **Numeracy Screener** free from Numerical Cognition Lab, CA
 - 2 activities: comparing dots, comparing numbers
 - Updated version more subtest, norms follow
- ❖ **Kindergarten Math CBM for fluency** Fuchs Research Group, Vanderbilt
 - Dots counting and easy calculations with written numerals
- ❖ **Early Numeracy Indicators ENI** free from the RIPM website
 - 4 subtests: read numbers, compare numbers, missing number, mixed
- ❖ **Universal Numeracy Screener USNS** free from Forefront Education
- ❖ **TEN Test of Early Numeracy** from AimswebPlus
 - 4 subtests: count, read numbers, compare numbers, missing numbers

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Numeracy Screener: www.numeracyscreener.org

WHO ARE WE ?

Numerical Cognition Laboratory

- Located within the [Department of Psychology](#) at Western University
- Part of the [Brain and Mind Institute](#)
- Directed by Dr. Daniel Ansari, consisting of graduate students and post-doctoral fellows from the fields of Psychology, Neuroscience, and Education
- We aim to better understand what predicts success and failures in early math learning
- Focus of our research is to gain a better understanding of how children develop numerical and mathematical competence

READ MORE

WHAT IS IT ?

A 2-4 minute test composed of two parts:

1. Symbolic (i.e. numerical digits)
2. Non-Symbolic (i.e. arrays of dots)

Developed by Drs. Nadia Howworthy & Daniel Ansari in the Numerical Cognition Laboratory at Western University

Measures a child's ability to understand numerical magnitude (quantity)

Correlations between performance on the Numeracy Screener and arithmetic skills have been demonstrated and published in scientific literature

These findings show that performance on the Numeracy Screener can explain individual differences in children's arithmetic skills

READ MORE

TAKE THE TEST

It's as easy as 1, 2, 3 ...

1. PRINT & FOLD THE TEST
Tests are provided in PDF format with detailed assembly instructions in both text and video formats
2. TAKE THE TEST
Administer the paper and pencil test and mark the scores
3. SUBMIT THE SCORES
Submit the scores and compare the child's performance to a norm of Canadian children's scores from senior kindergarten through to grade 3

IM READY

26

2 sections:
dots,
numerals

spring KG:
2 min per
section,

1st - 2nd grade:
fall, winter,
spring: 1 min.
per section

practice page

Mark the box with the largest number or the most dots

D

E

F

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Screen student

Recommended Tests for Kindergarten 1:

Digit Comparison 1-9

Addition Small Test

Mixed Comparison

Number Line Estimation 0-10

Number Recognition

Subtraction Small Test

All Tests

Number Processing Tests

Digit Comparison 1-9

Dot Comparison 1-9

Mixed Comparison

Dot Comparison Large

Digit Comparison Large

Number Recognition

Number Line Estimation 0-10

Number Line Estimation 0-50

All Tests

Selected Tests

Digit Comparison 1-9

Dot Comparison 1-9

Dot Comparison Large

Digit Comparison Large

Addition Small Test

Subtraction Small Test

Addition Large Test

Subtraction Large Test

Number Recognition

Number Line Estimation 0-10

Number Line Estimation 0-50

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NumeracyScreener.com tutorial
NumeracyScreener.app to do the test online

- Digit comparison (2 levels)
- Dot comparison (2 levels)
- Mixed comparison
- Number recognition
- Number line estimation (2 levels)
- Addition (2 levels)
- Subtraction (2 levels)

Single Digit

Mixed

Symbolic

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Progress monitoring

Visualize Data

You are viewing summarized test results for all students. Use the filter below to view data for specific tests.

All Groups

Group

Student

Test Selection

Digit Comparison 1-9

Group: Dr. Daniel Ansari's Classroom

Student: 1

Correct Items Over Total Items By Attempt

57 Items

68 Items

Progression of Scores (Correct/Attempted Items)

96.1%

64.06%

30

Kindergarten Math Computation Fluency: 5 min

KINDERGARTEN

MATH CBM

COMPUTATION FLUENCY

+

=

4 + 0 =

☆

☆

☆

☆

=

2 + 3 =

• •

• •

• • + • =

3 - 0 =

• • • • •

• • • • •

Cross out 5

• • • • •

• • • • •

• •

• •

1 + 2 =

5 - 1 =

By Seethaler and Fuchs, Vanderbilt University

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Early Numeracy Indicators,
mixed examples

5

2

7

1

8

3

0

1

2

1

3

4

5

10

15

6

15

1

44

Fall

Winter

Spring

Date

Number Identification

Form 1

Form 2

Mean

Quantity Discrimination

Form 1

Form 2

Mean

Missing Number

Form 1

Form 2

Mean

Mixed Numeracy

Form 1

Form 2

Mean

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Early Numeracy AIMSweb PLUS, 1st grade

MEASURE	TIME	GRADE	FALL	WINTER	SPRING	Prog. Mon.
Number Naming Fluency	1 min.	k	x	x	x	x
Quantity Dots - Total Fluency	1 min.	k	x	x	x	x
- Difference Fluency	1 min.	k		x	x	x
Concepts & Applications: Mental Math	7-12 min.	k, 1	x	x	x	
Number Comparison Fluency	1 min.	1	x	x	x	x
Math Facts Fluency – 1 Digit	1 min.	1	x	x	x	x
– Tens	1 min.	1		x	x	x

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Language

Oral expression

Listening comprehension

Written expression

Basic reading skills

Reading fluency skills

Reading comprehension

Math

Mathematics calculations

Mathematics problem solving

IDEA SLD

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Language

Oral expression

Listening comprehension

Written expression

Basic reading skill

Reading fluency

Reading comprehension

Math

Count, mental math

Verbal math concepts

Written calculations

Read numbers and signs

Calculation fluency

Understand written concepts, formulas

Math problem solving

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National Council of Teachers of Mathematics
NCTM

Teaching and learning

• Conceptual understanding

• Procedural Fluency

• Strategic competency

• Adaptive reasoning

• Productive disposition

Strands

• Number and Operations

• Algebra and patterns

• Geometry

• Measurement

• Data analysis and probability

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Mathematics calculation

- Counting forward, backward
- Read and write numerals
- Number comparison
- Number patterns
- Understand place value
- Know basic math facts
- Add, subtract, multiply, divide
- Whole numbers, fractions, decimals, powers, roots, etc.
- Use models and number lines
- Algorithms and formulas
- Round, estimate, and check

Mathematics problem solving

- Verbal comprehension
- Understand the process:** is a quantity added, subtracted, multiplied, split etc.?
- Multistep questions** require working memory, planning, and sequencing
- Strategies:** draw a picture, work backwards, act it out, find a pattern, make a table, solve a simpler problem, logical reasoning, use a graph, write a number sentence, guess and check
- Apply calculations**

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Typical calculation format in achievement tests

6 + 4 = ?

9 - 6 = ?

3 x 5 = ?

20 : 4 = ?

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All formats required by the NCTM

6 + 4 = ?

9 - 6 = ?

3 x 5 = ?

20 : 4 = ?

6 + ? = 10

9 - ? = 3

3 x ? = 15

20 : ? = 5

? + 4 = 10

? - 6 = 3

? x 5 = 15

? : 4 = 5

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LDA

Learning Disabilities Association of America

THE LD INSTITUTE

Learning Disabilities Association of America

INDEPENDENT OF AMERICA

SALT Center

SUPPORT EDUCATE ADVOCATE

The LDA published the Specific Learning Disabilities Evaluation Principles and Standards

Resource: Connect the CHC to Intervention Tools

<https://ldaamerica.org/the-ld-institute>

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LDA: SLD Evaluation Principles and Standards

Inter-disciplinary

Dynamic, iterative

Literacy and numeracy research

Cultural background

Strength based

Professional development

Effective instruction

Focus on improved outcomes

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Guidance for the Comprehensive Evaluation of Specific Learning Disabilities

TEA

Texas SPED Support

Texas SLD identification

1. Determination by MDT

2. Observation of student's learning in areas of difficulty

3. Documentation of inadequate achievement based on multiple sources

4. Verification of appropriate instruction

5. Examination of exclusionary factors

6. Confirmation of insufficient progress based on response to scientific research-based intervention OR a pattern of strengths and weaknesses

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TEA eligibility criteria: SLD

DO need a pattern of strengths and weaknesses in performance, achievement, or both

That pattern is relative to age, grade-level standards, or intellectual development

DO NOT need significant variance among specific areas of cognitive functioning or between specific areas of cognitive function and academic achievement

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INFORMAL

- Referral Data
- Records Review
- Vision/Hearing Screening
- Work Samples
- Parent Information/Interview
- Teacher Information/Interview
- Observations - School/Home

CURRICULUM-BASED

- Teacher-made/Textbook Quiz
- District Benchmarks
- Curriculum Based Measurement (CBM)
- Running Records
- Progress Monitoring
- Universal Screeners

CRITERION-REFERENCED

- State of Texas Assessments of Academic Readiness (STAAR®) and STAAR Alternate (ALT) 2
- Universal Screeners
- Iowa Test of Basic Skills (ITBS)
- Brigance Test
- Texas English Language Proficiency Assessment System (TELPAS) and TELPAS ALT
- Advanced Placement (AP) Tests
- Scholastic Aptitude Test (SAT) and American College Test (ACT)

NORM-REFERENCED

- Standardized Measures:
 - Achievement Tests
 - Cognitive Tests
 - Developmental Measures
 - Specialized Measures

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Achievement data sources

INFORMAL

- Parent information/ interview
- Teacher information/ interview
- Observation
- Student information/ interview
- Work samples - math journals, single-skill calculation tasks, mixed-skill calculation tasks, math fluency tasks

CURRICULUM-BASED

- Teacher-made tests/ quizzes
- Intervention progress monitoring
- CBM – early numeracy, computation (available via [Intervention Central](#))
- Comparison to enrolled grade-level standards
- [Mathematics Progress Monitoring Measures](#)

CRITERION-REFERENCED

- Math universal screeners
- District math benchmarks
- STAAR® math assessment

NORM-REFERENCED

Standardized measures of math calculation (timed and untimed)

Standardized measures of word problems (orally presented), graphs/ tables, measurement tasks, time and money concepts

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KG - 1

Counting late

Not counting back

Low sequencing

Part-Part-Whole

Subitizing, dice

Less interest in ordering, sorting, dice, dominoes, blocks, puzzles, patterns, games

2 - 3

Keeps counting by 1

Low number sense

Adds all, not adds-on

Can't memorize add or subtraction facts

Number lines are confusing

Only place value name, no regrouping skills

Left-Right, directions

Analog clock is hard

4 - 6

Still counting, tally marks

Multiplication tables low

Word problems confusing

Struggles with fractions, decimals, percentages

Can't make a sensible guess, answers are far off

Fraction, decimal, percent

Proportional thinking

Works slowly, anxiety

Time, money, direction

Forget numbers, data, login

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Middle school

Lacks vocab, procedures, concepts

Fractions, decimals, percentages difficulties

No proportional reasoning

No connection between representations

Word problems: no reality check if answer 'makes sense', can't estimate

Low organization in general

Loses dates, deadlines, log ins

High School

Abstract reasoning deficit

Can't relate a concrete situation with algebraic expression

Can't generalize

Difficulty with the ways two quantities can be connected

Does not see a patterns

Can't visualize shapes, tables, and graphs in geometry

Difficulty with the language of math, notations, formulas

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Assessment Name	Provider	Cost/student	Frequency	Length
AMU grades K-2	Educ. NW	free	3	20-30 min.
Fastbridge Math	Renaissance	\$8.00	3-5	15-30 min.
i-Ready Diagnostic	Curr. Ass.	\$8.00	3	25-60 min.
IXL Math (Not KG)	IXL	\$13.25	3	20-30 min.
mClass Math	Amplify	\$9.00	3	30 min.
NWEA MAP GROWTH	NWEA	\$7.50	3-5	45 min.
AIMSweb Plus	Pearson	\$4.25	3-5	K-1 15 min. 2-12 25-35 min.
Star Math	Renaissance	\$5.41	3-5	25-30 min.

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Easy CBM tests: K–8 and Proficient math, free
monthly progress with graph: easycbm.com

K

Numbers and Operations; Geometry; Measurement

1

Numbers and Operations; Geometry; Measurement and Data

2-3

Numbers and Operations; Geometry; Algebra

4-5

Numbers and Operations; Measurement; Algebra; Data

6-8

Numbers and Operations; Algebra; Geometry/Measurement

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NWEA MAP test: K–12, 45 – 60 min.

K-2

- Operations and Algebra: Solve Problems; Operations, Properties
- Number/Operations: Place Value, Counting, Base Ten, Fractions
- Measurement, Data: Problems Involving Measurement and Data
- Geometry: Reason with Shapes and Their Attributes

2-5

- Operations and Algebra: Solve Problems; Patterns, Relationships
- Number and Operations in Base Ten and with Fractions
- Measurement and Data; Geometric Measurement and Problems
- Geometry: Reason with Shapes, Attributes, & Coordinate Plane

6+

- Ratios and Proportional Relationships
- Expressions and Equations
- Geometry

The Number System
Functions
Statistics and Probability

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Parameters in FIE reports

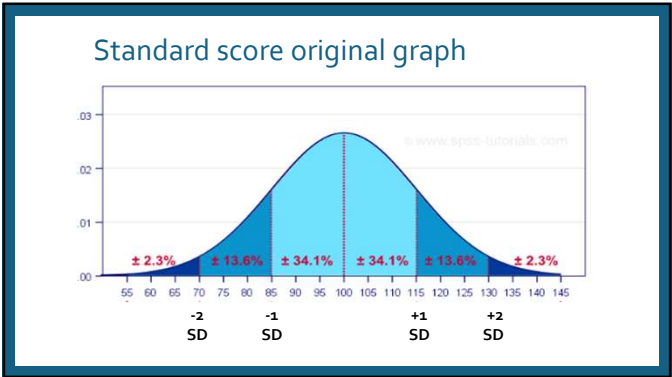
General ability tests

- Standard Scores and confidence interval
- Percentile ranks (related to SS)
- Significant differences

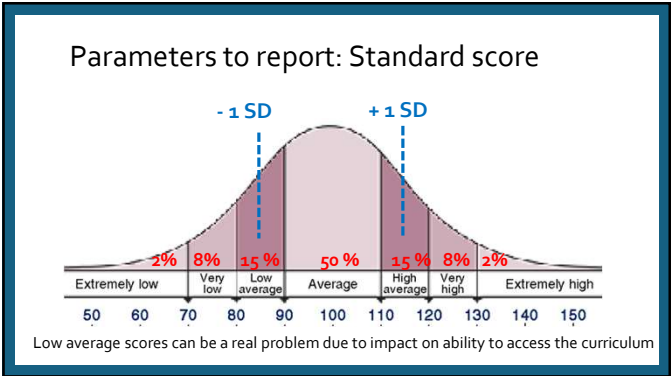
Achievement Tests

- Standard Scores and confidence interval
- Percentile ranks (related to SS)
- Relative Proficiency Index
- Grade equivalent/Age Equivalent

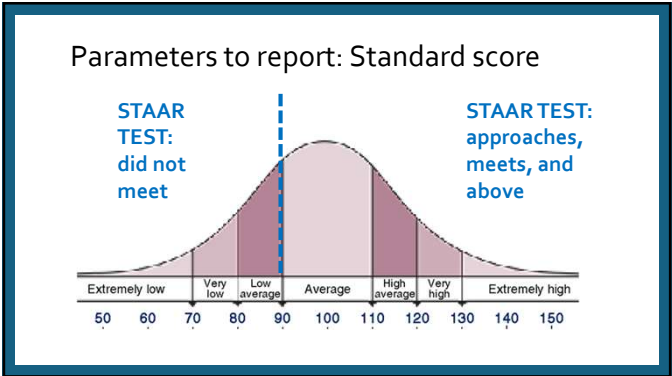
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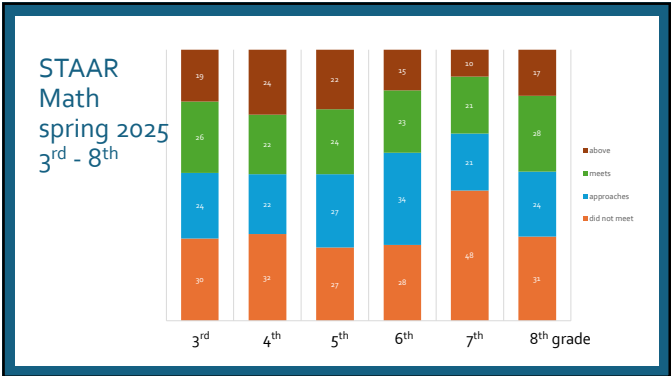
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Relative Proficiency Index

Grade Equivalent

- Criterion referenced
- The score the assessed student would get for similar test questions for which an average performing student would score 90
- Common RPI is 82-95

- The earliest grade level at which an average performing student would get this question correct

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Cognitive abilities

Achievement

•CAS-2: 5-18	•KTEA-3 preK-12
•KABC II-NU 3-18	
•TONI-4 6-90	
•CTONI-2 6-90	
•WISC-5 6-16	•WIAT-4 PreK-adults
•W-JV COG 5-90	•W-JV ACH 5-90
•CB-TT 6-90	•WRAT-5: 5-85
•Panamath 6-90	

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Cognitive abilities

Achievement

•CAS-2: 5-18	•KTEA-3 preK-12
•KABC II-NU 3-18	
•TONI-4 6-90	
•CTONI-2 6-90	
•WISC-5 6-16	•WIAT-4 PreK-adults
•W-JV COG 5-90	•W-JV ACH 5-90
•CB-TT 6-90	•WRAT-5: 5-85
•Panamath 6-90	

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Corsi Block-Tapping Test

- Visual spatial short-term memory: repeat tapping forward
- Visual spatial working memory: tap blocks backward

Examinee's view online

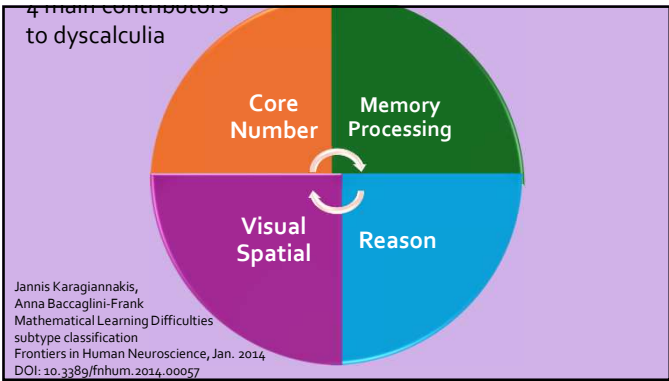
Examiner's view in person

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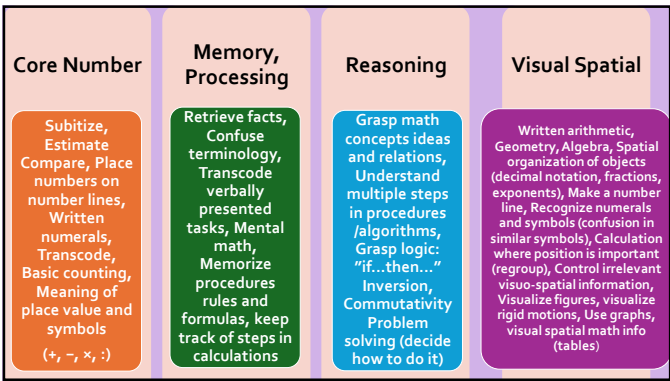
◆ Gs with strong links with Math LD

Gc Crystallized intelligence	◆ Gf Fluid reasoning	◆ Gsm Short term memory
◆ Glr Long-term retrieval	◆ Gv Visualization	◆ Gs Perceptual speed
◆ Gq Quantitative knowledge	Glr Naming facility	Ga Auditory processing

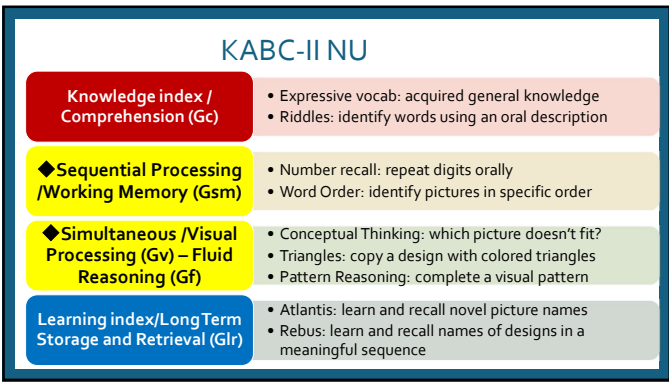
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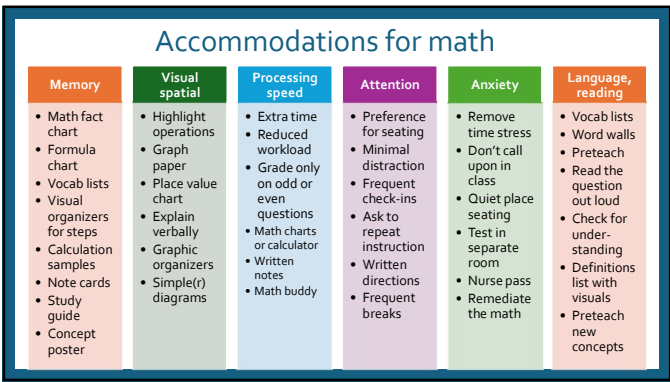
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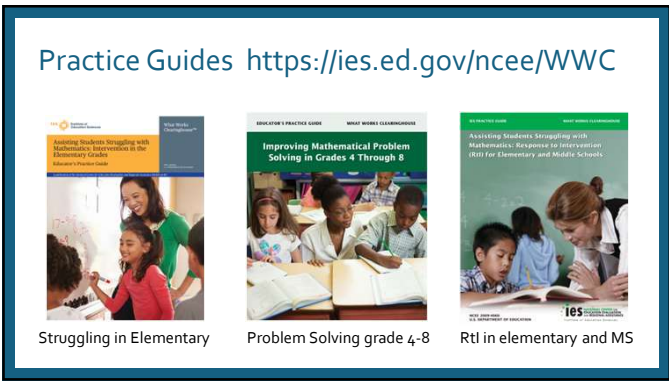
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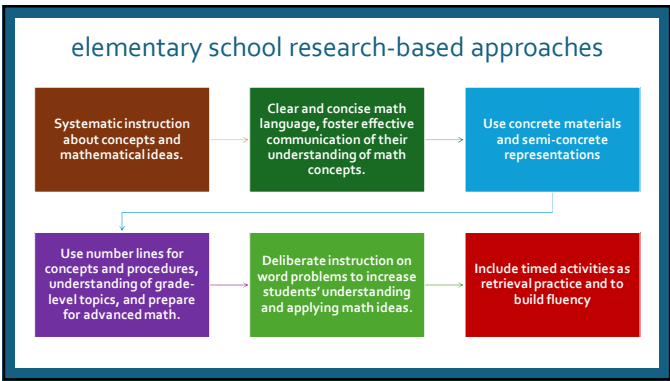
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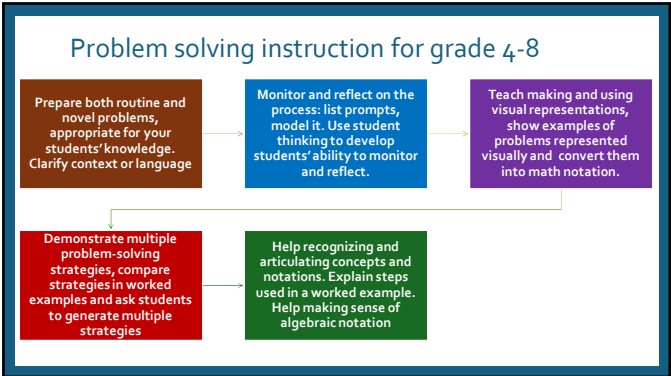
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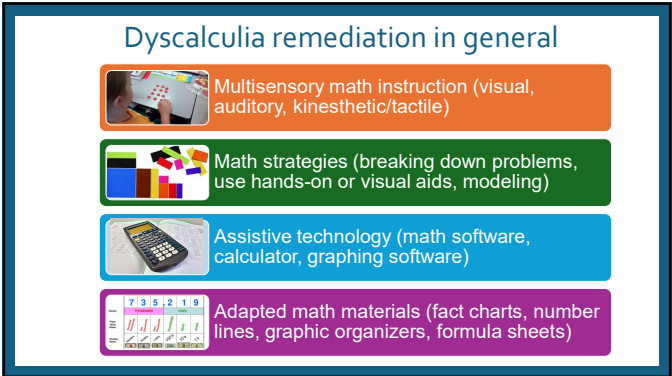
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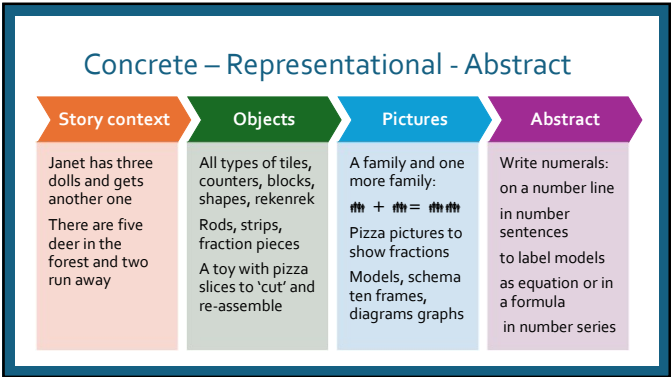
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67



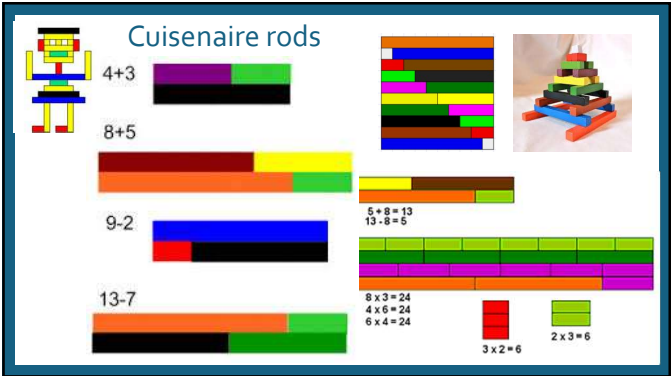
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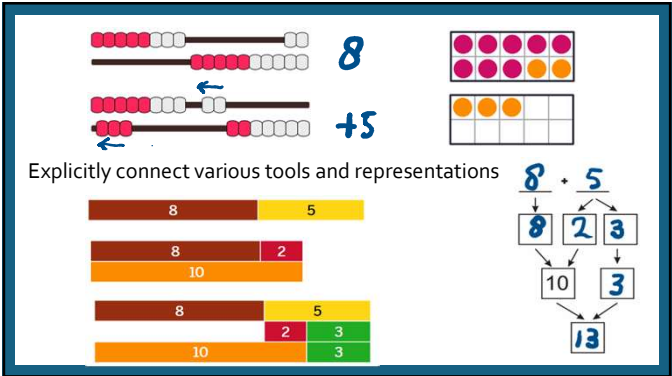
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Topic								
Count/subitize	✓	✓	✓	✓				
Add/subtract	✓	✓	✓	✓				
Multiply		✓	✓	✓	✓			✓
Divide		✓	✓	✓				✓
Fractions				✓		✓	✓	
Decimals					✓		✓	
Proportions					✓	✓		✓
Algebra						✓	✓	✓
Geometry						✓	✓	✓

70

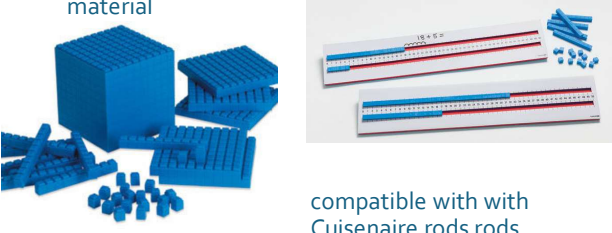


71



72

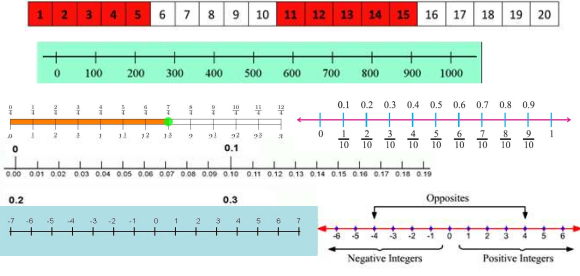
interlocking base ten blocks
hands-on 'building' like Lego's to regroup, and
split up again, instead of changing out
material



compatible with with
Cuisenaire rods rods

73

Developing number line concepts



0 100 200 300 400 500 600 700 800 900 1000

0 1 2 3 4 5 6 7 8 9 10

0.1 0.2 0.3 0.4 0.5 0.6 0.7 0.8 0.9

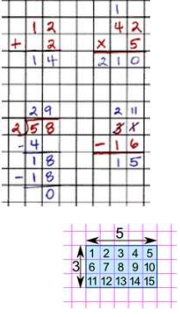
0.00 0.01 0.02 0.03 0.04 0.05 0.06 0.07 0.08 0.09 0.10 0.11 0.12 0.13 0.14 0.15 0.16 0.17 0.18 0.19

0.2 0.3

Opposites

Negative Integers Positive Integers

74

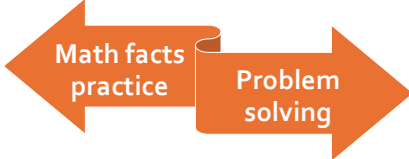


Graph paper is indispensable

- One number or sign per square
- Match for handwriting size
do2learn.com, printablepaper.net
- Keeps numbers aligned, helps with regrouping, place holder zeros don't get lost, shows concept of place value
- Draw models, rectangles to multiply, area and perimeter, quadrilaterals
- Draw strip models and fraction strips
- Geometry, graphs, functions

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Word problems: separate first, combine later



Math facts practice Problem solving

NumberlessWP.com

1.Product? 2. Number of groups? 3. Group size ?

76

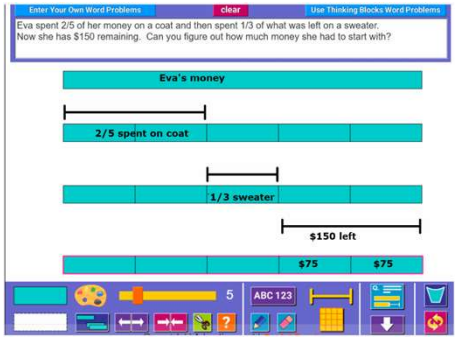
Sample problem that needs modeling from
the Problem Solving grade 4-8 Guide, p.24

- Eva spent $\frac{2}{5}$ of her money on a coat and then spent $\frac{1}{3}$ of what was left on a sweater.
- Now she has \$150 remaining.
- Can you figure out how much money she had to start with?



Next slide how you can demonstrate with free strip models
on MathPlayground.com Story problems Thinking Blocks

77



Enter Your Own Word Problems clear Use Thinking Blocks Word Problems

Eva spent $\frac{2}{5}$ of her money on a coat and then spent $\frac{1}{3}$ of what was left on a sweater. Now she has \$150 remaining. Can you figure out how much money she had to start with?

Eva's money

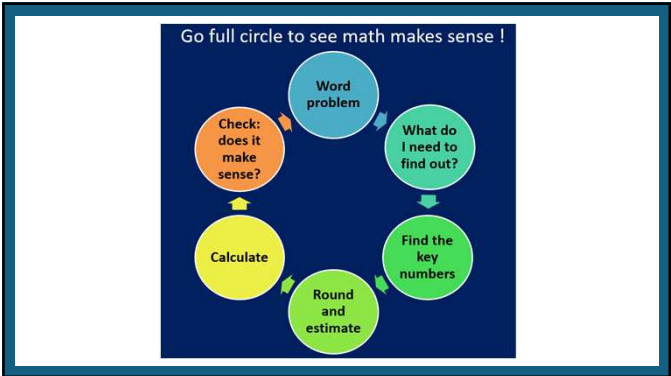
$\frac{2}{5}$ spent on coat

$\frac{1}{3}$ sweater

\$150 left

\$75 \$75

78



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MDT



Updated Guidance for the Comprehensive Evaluation of Specific Learning Disabilities



- When dyslexia is suspected, a person with specific knowledge in the reading process, dyslexia and related disorders, and dyslexia instruction must serve on the LEA's multidisciplinary team and any ARD committee that is convened to determine eligibility for special education and related services.

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weak

Reason

Visual

strong

Verbal

Speed

Memory

Use strengths:
Explicit verbal explanations
Mnemonics, Acronyms,
Word walls, Definitions list
Skip counting
Chunking information
Cover-Copy-Compare

To develop weaknesses:
Break down reasoning in small verbal parts, list the steps
Explain and label models verbally
Spent more time on practicing visual structures: number lines, shapes, graphs and relearn them

81

weak

Speed

Memory

strong

Visual

Reason

Verbal

Use strengths:
Use modeling to teach new concepts
Present info diagrammatic
Number line to explain calculations
Reason from known fact to new fact
Connect concepts visually

To develop weaknesses:
Use graphic organizers to help memorizing steps, also train to memorize the layout of the organizer
Use Cloze technique for formulas
Speed training with cards temporarily
Favoring speed over exactness
Cover-Copy-Compare for memory

82

Box model for multiplication

23×14

20	3
200	30
80	12

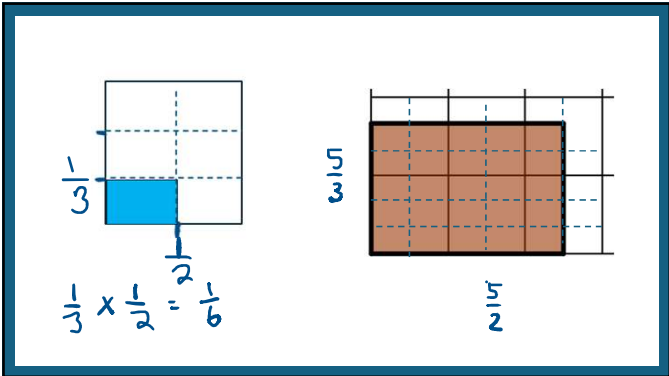
$200 + 30 + 80 + 12 = 322$

83

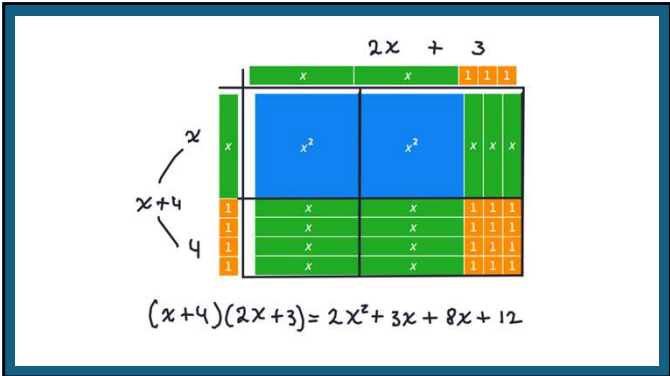
$\frac{1}{3} \times \frac{1}{2} = \frac{1}{6}$

$2\frac{1}{2}$

84



85



86

Remediation programs selection					
Program	grades	group	time	cost	Effect size
CTL Whole Number Foundations (Roots)	K-1	2-5	20 min. 50 lessons	\$540	+0.18
Bridges intervention, Math Learning Center	K-2 3-5	small group	30 min. 40-65 lessons per volume	\$1,100 \$1,100	+0.10-0.25
M-STAR 1. Math Facts Multiply and Divide 2. Equivalent fractions 3. Ratios 4. Proportionality	Elem./MS		30 min. at least or 2-3 day, 12 lessons >30 min. 15 lessons >30 min. 11 lessons >30 min. 17 lessons	free	
EduGAINS Canada GAP Closing	MS,HS	small group	3-10 sections in 7 modules	free	

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Remediation programs Fuchs Research Group					
Program	grades	group	time	cost	Effect size
Galaxy Math	1-3	1-3	3x 30 min. 15 weeks	\$75-90	+0.29
Pirate Math individual whole class	1-3 1-3	1-3 class	3x 30 min. 13 weeks	\$75-95	+0.37
Math Wise Calculation	2	1-3	2x 45 min. 17 weeks	\$130	+0.34
Number Rockets	2-4	1-3	3x 40 min. 17 weeks	\$130	+0.34
Fraction Face Off Super Solvers Fraction	4 4-5	2-4	3x 30 min. 12 weeks 45 min. 29 lessons	\$130 \$125-150	+0.59

88

Counting on a number line
Identifying numbers smaller and larger than a given number
Defining key mathematical terms
Introducing tools for addition and subtraction
Utilizing families of numbers for addition and subtraction
Galaxy Math incorporates a space theme to increase student interest

Lynn S. Fuchs, Douglas Fuchs, Caitlin Craddock, & Pamela Seethaler
Vanderbilt University

frg@vanderbilt.edu

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Fully scripted, easy to use, teaching assistant
Proven effective: effect size 0.37
16 weeks, 48 lessons, 25-30 minutes
Includes all instructional materials, instructor provides stopwatch/timer, reinforcers treasure chest
Structure:
2-4 min. math flashcards
2-3 min. warm up, reteaching
15 min. scaffolded instruction
3 min. sorting cards timed practice
5 min. pen and paper problem solving

Lynn S. Fuchs, Pamela M. Seethaler, Sarah R. Powell, and Doug Fuchs
Vanderbilt University

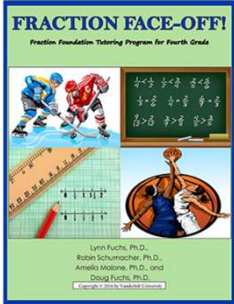
frg@vanderbilt.edu

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Identify and write numbers
Identify more and less objects
Sequence numbers
Use $<$, $>$, and $=$ signs
Skip counting by 10s, 5s, and 2s
Identify place value
Identify operations
Write addition and subtraction sentences
Learn addition and subtraction facts
Learn two-digit addition and two-digit subtraction
Learn missing addends

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Tier 2 intervention
measurement interpretation of fractions (magnitude)
comparing and ordering fractions,
placing fractions on a 0 -1 number line,
adding and subtracting fractions, word problems
finding fractions = $\frac{1}{2}$ with multiplication;
finding fractions = 1 with multiplication,
converting mixed to improper and vv.

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Fractions 4th and 5th

Comparing two fractions
Ordering three fractions
Placing fractions on a 0-1 and 0-2 number line
Solving fraction word problems
Solving fraction calculation problems

93

Fluency.Amplify.com

How many more make 10? $\star$

$6 + ? = 10$

$6 \times ? = 30$

$5 \times 4 = ?$

$4 - 1 = ?$

Multiplication by Heart
These beautiful flash cards use spaced repetition to teach multiplication facts. Achieve fluency with just five minutes of practice per day!

94

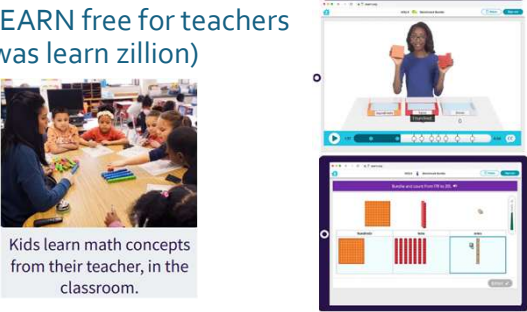


HappyNumbers.com K-5
illuminations.nctm.org K-12
khanacademy.org/kids PreK-2
matific.com K-6
zearn.org K-5
stmath.com K-8

95

ZEARN free for teachers
(was learn zillion)

Kids learn math concepts from their teacher, in the classroom.



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Impact statement SLD in Math

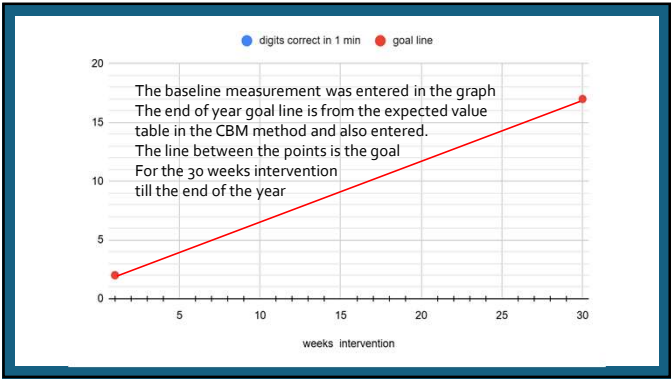
- Nadia shows below average progress in Math: below 25% mastery on grade benchmark assessments, which is causing frustration
- On an untimed single-digit pen and paper add and subtract test she solved 25% correctly; she drew dots next to the numbers
- When using counting cubes, she solved 67% correctly, but took longer
- Her LD in math limits her ability to do single-digit addition and subtraction in a timely fashion,
- Her limited memory results in difficulties to commit math facts to memory
- Currently Nadia is not able to keep up with the curriculum due to lack of accuracy and automaticity and urgently needs intervention using hands-on materials, pictorial representations, and written numerals.

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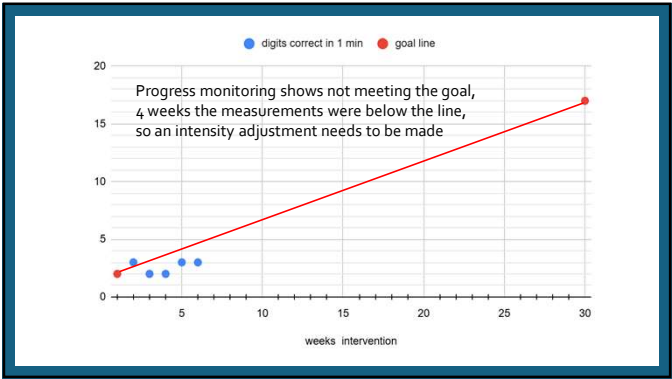
Options for frequent progress monitoring

- EasyCBM.com Grade K-8, EasyCBM.com University of Oregon
- Monitoring Basic Skills Progress Calculations Grade 1-6, Pro-Ed
- Fractions CBM Fuchs Research Group, Vanderbilt University
- AAIMS Algebra progress monitoring Iowa State University
- Online: M-COMP (computation) and M-CAS (concepts and skills)

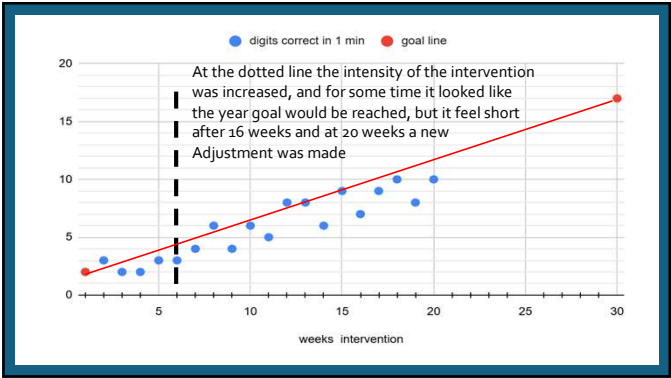
98



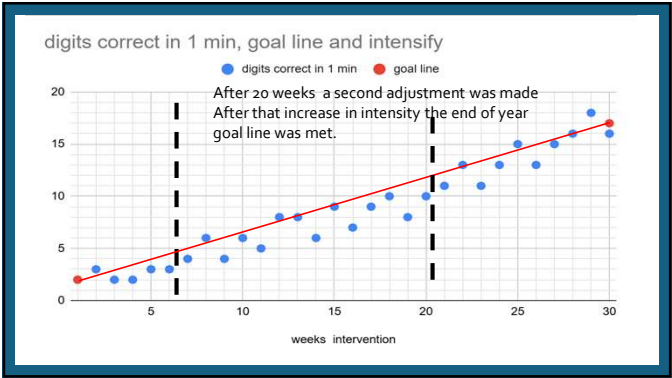
99



100



101



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IEP goals: add, subtract, multiply, word problems

- Given ten three-digit addition and subtraction problems, Matteo will add and subtract within 1,000 using strategies and algorithms based on place value, properties of operations, and/or the relationship between addition and subtraction as measured by teacher records or observations or test with 80% accuracy by the end of the year
- Matteo will multiply and divide within 100, using strategies such as the relationship between multiplication and division as measured by teacher records, observations, or test with 80% accuracy by the end of the year
- Matteo will fluently solve mixed operation calculations of third grade level at a rate of 18/min of correct answers by the end of the year
- After schema instruction, Matteo will solve one- and two-step word problems in situations involving equal groups, arrays, and measurement quantities with 75% accuracy as measured by teacher records, observation, or test by the end of the year
- Matteo will accurately measure common classroom items in whole and half inches using a ruler

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WIAT Error Analysis to Goals samples

- Single-operation word problems: General, Time, Money
- Annual Goal
 - Given ____ word problems involving a single operation of addition, subtraction, multiplication, or division with one or more (circle: two-digit or three-digit) numbers, the student will write or say the solutions with no more than ____ errors.
 - Example: David needs \$149 for a game, he has \$95. How much more does David need to save? (Student writes/says: 54.)
- Short-Term Objective
 - Given ____ word problems involving a single operation of (circle: addition, subtraction, multiplication, division) with single-digit or two-digit numbers, the student will find the solutions with no more than ____ errors.
 - Example: David had 29 old shirts, and he gave 14 to his brother. How many old shirts does David have? (Student writes/says: 15.)

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Learning multiplication strategies: doubles, split in smaller multiplications from NCTM

3 groups of 4, or 4 taken 3 times

3 rows of 4, or 3 x 4

4 columns of 3, or 4 x 3

$2 \times 7 = 14$
 $2 \times 7 = 14$
 $4 \times 7 = 28$

8×6

$8 \times 5 = 8 \times 1$

$5 \times 8 = 40$ five 8s

$2 \times 8 = 16$ two 8s

$7 \times 8 = 40 + 16 = 56$ seven 8s

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Fractions Curriculum-Based Measurements

Super Challenge Graph

Score

Super Challenge

By Lynn Fuchs et al Vanderbilt university

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Example impact statement MS math

- According to a recent diagnostic math assessment, Amy performs at a 5th grade level. Amy is currently **not passing** her 8th grade Pre-Algebra class. Math is the area that Amy needs the most support. She received a **did not meet score on the Math STAAR test**, while RLA scored above
- She currently receives math services for 20 minutes daily in a small group. The teacher reports that **frequent review** of concepts and materials presented in small increments is the most effective method. Amy fluently retrieves basic math facts, can do **operations with whole numbers, equality of fractions and decimals**, with **verbal explanation** but struggles to setup proportions to solve problems, to divide with fractions, and all 4 basic operations with integers. She has difficulties with operations with mixed numbers and percentages especially multi step word-problems, which will affect her involvement and progress in the general curriculum.

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Impact statement 2

- Results of a recent benchmark test indicate that she continues to need specialized instruction in the areas of solving practical problems, proportional relationships, division with fractions, expressions/operations, order of operations, exponents/squares and square roots, and plane and solid figures.
- Although Amy continues to work toward grade-level proficiency, it is unlikely to achieve this in one year

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Measurable IEP Math goals examples

- 1. When provided a graphic organizer, Amy will be able to **compare and order (ascending and descending) three to five fractions, decimals, percentages**, as measured by classroom assignments, teacher observation and test, with **85% accuracy** by the end of the school year.
- 2. Given a graphic organizer, Amy will be able to apply the **order of operations** to **simplify numerical expressions with square numbers and square roots, fractions, decimals, and integers**, as measured by classroom assignments and tests, with **75% accuracy** by the end of the school year.
- 3. After schema-based instruction, Amy will be able to solve **single-step and two-step practical problems by using computation procedures for whole numbers, integers, fractions, and decimals**, as measured by classroom assignments, teacher observations and tests, with **75% accuracy** by the end of the school year.
- 4. Using concrete materials and pictorial representations, Amy will be able to **solve two-step linear equations and inequalities**, as measured by classroom assignments, observations, and tests, with **80% accuracy** by the end of the school year.

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Summary Dyscalculia: The Core Deficit

- Dyscalculia** is a deficit in "number sense," including subitizing, magnitude comparison, and estimation.
- The Mental Number Line:** Difficulty developing a mental number line that represents size and length.
- Difficulties:** with basic math facts (only count), place value, word problems, proportional thinking, graphs, models

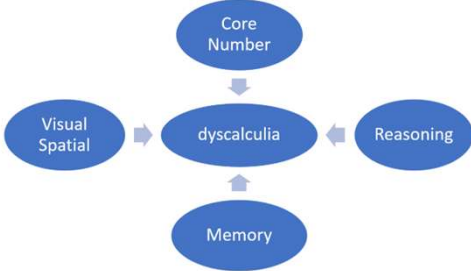
110

Developmental Dyscalculia

- starts early on in math: screen all kids in KG and 1st grade, early intervention is most effective
- it exists on a sliding scale, with each individual experiencing unique manifestations, common comorbidities dyslexia, dysgraphia
- inborn, it runs in families
- most current tests are not covering all components yet
- we need more resources



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```
graph TD;
    CoreNumber([Core Number]) --> Dyscalculia([dyscalculia]);
    VisualSpatial([Visual Spatial]) --> Dyscalculia;
    Reasoning([Reasoning]) --> Dyscalculia;
    Memory([Memory]) --> Dyscalculia;
```

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effective intervention strategies & methods

- Practice Guides: <https://ies.ed.gov/ncee/WWC>
- Galaxy Math, Number Rockets, Pirate Math, Fraction Face-Off, Brain Boost: frg@vanderbilt.edu
- M-STAR intervention, Meadows Center Austin
- GAP closing Edugains Canada
- Online: Happy Numbers, ST MATH, Zearn, Matific, Amplify

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Q and A



Feel free to email me with any questions
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drschreuder@dyscalculiaservices.com
DyscalculiaTutorTraining.org

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